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Development of a large-scale single U.S.
region CGE model using IMPLAN data:
A Los Angeles County example with a
productivity shock application

by

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A Los Angeles County example with a productivity shock application**

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Abstract

This paper details the construction of a large-scale computable general equilibrium (CGE) model for a single U.S. region. The model contains detailed treatment of margins and taxes, features not typically given prominence in U.S. regional CGE models. The starting point for the core of the CGE model's data base is information from IMPLAN, producers of regional I/O data at the U.S. county and state levels. IMPLAN's I/O tables, however, are in producer prices with aggregated treatment of margins and taxes. The methods for reconfiguring the I/O data into basic price flows with direct allocation of imports and a disaggregated treatment of taxes and margins are described. The method is applied to construction of a Los Angeles County model. An illustrative simulation of a productivity improvement in the Los Angeles County economy is then discussed.

JEL Classification: C68, R13, R15

Key words: regional CGE, IMPLAN.

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1. INTRODUCTION

IMPLAN (Minnesota IMPLAN Group 1997) is a widely-used data resource for undertaking input-output analysis at the U.S. sub-regional level. ORANI-G (Horridge 2003) is a widely-used template for a detailed single-region CGE model. This paper uses IMPLAN data, together with share and parameter values from USAGE¹, to construct a single-region CGE model for a small U.S. region. To make ORANI-G (a single country model) suitable for implementation at the small region level, a number of theoretical modifications to the standard ORANI-G framework are necessary. These are described in Section 2. The resulting model is called ORANI-R. Section 3 describes the development of the ORANI-R database from IMPLAN data. The specific implementation is Los Angeles County. Section 4 presents an illustrative simulation with the new model: short-run and long-run productivity growth in the Los Angeles County economy.

2. A SUB-NATIONAL IMPLEMENTATION OF THE ORANI MODEL

2.1 ORANI-R model overview

The well-known ORANI-G model is used as the starting point for the development of a single-region sub-national model, ORANI-R. The structure of ORANI-R is identical to that of ORANI-G in all respects other than those outlined in Section 2.2. Full documentation of the theoretical structure of ORANI-G and its antecedent, ORANI, are available in Horridge (2003) and Dixon *et al.* (1982) respectively.

ORANI-R is a single-region sub-national comparative-static computable general equilibrium model. The model features detailed sectoral disaggregation. For example, the Los Angeles County implementation developed in this paper covers 436 sectors and 19 margin commodities. Familiar neoclassical assumptions govern the behaviour of the model's economic agents. Decision-making by firms and households is governed by optimising behaviour. Each representative industry is assumed to minimise costs subject to constant returns to scale production technologies and given input prices. Household commodity demands are modelled via a representative utility-maximising household. Units of new industry-specific capital are assumed to be cost minimising combinations of commodities sourced from the local region, the rest of the U.S. and overseas. Imperfect substitutability between local, rest-of-U.S. and foreign varieties of each commodity are modelled via CRESH² aggregation functions. Inter-regional and foreign export demands for local commodities are modelled via commodity- and destination-specific constant elasticity export demand schedules. The model recognises the consumption of commodities by state and federal government. A variety of direct and indirect taxation instruments are identified. Domestic commodity markets are assumed to clear and to be competitive. Purchasers' prices differ from basic prices by the value of indirect taxes and

¹ USAGE is a detailed, dynamic CGE model of the U.S. It has been developed at the Centre of Policy Studies, Monash University, in collaboration with the U.S. International Trade Commission. Prominent applications of USAGE by the U.S. International Trade Commission include USITC (2004 and 2007)

² Hanoch (1971).

margin services. The model is solved using the GEMPACK economic modelling software (Harrison and Pearson, 1996).

2.2 Development of a sub-national implementation of ORANI-G

To date, ORANI has only been implemented as a national model. To implement the ORANI model at the sub-national level, new theory must be added to the core model to determine:

- (i) short-run and long-run regional labour supply;
- (ii) the price of interstate imports;
- (iii) the price of interstate exports;
- (iv) imperfect substitution between commodity varieties.

These developments are discussed below.

2.2.1 Short-run and long-run regional labour supply

A typical labour market closure for a single-country short-run implementation of the ORANI model assumes endogenous national employment with an exogenous real consumer wage. This setting is suitable for short-run modelling of countries with centralised wage setting arrangements and moderate or high unemployment. It is less suitable in situations of decentralised wage setting and low unemployment. As such, the single-region U.S. implementation of ORANI-G proposed in this paper establishes a regional labour market theory and closure that allows simultaneous stickiness in short-run employment and wages. This better-reflects a short-run situation of low unemployment, stickiness in regional migration, and wage flexibility: characteristics of the U.S. labour market³. The following four equations describe the regional labour market:

$$(1) \text{ pprate} = \alpha_{\text{PPRATE}} \times \text{realwage} + f_{\text{PPRATE}}$$

$$(2) \text{ emprate} = \alpha_{\text{EMPRATE}} \times \text{realwage} + f_{\text{EMPRATE}}$$

$$(3) \text{ hours} = \alpha_{\text{HOURS}} \times \text{realwage} + f_{\text{HOURS}}$$

$$(4) \text{ pop} = \alpha_{\text{POP}} \times (\text{realwage} - \text{frealwage}) + f_{\text{POP}}$$

$$(5) \text{ employ} = \text{pop} + \text{shwrkage} + \text{pprate} + \text{emprate} + \text{hours}$$

where:

³ It also facilitates short-run exogenous shocks to regional labour supply, something not possible under an assumption of exogeneity of the real regional wage. Impetus to development of ORANI-R was a desire to investigate the economic consequences of disaster and terrorism events at Center for Risk and Economic Analysis of Terrorism Events, University of Southern California. Some such events involve mass casualties. Labour supply shocks arising from such casualties are impossible under the standard regional labour market closure of effective exogeneity in the regional wage.

$pprate$	is the percentage change in the regional participation rate;
$realwage$	is the percentage change in the regional real wage;
f_{PPRATE}	is a shifter on equation (1), typically exogenous;
$emprate$	is the percentage change in the regional employment rate (1 – the unemployment rate);
$f_{EMPRATE}$	is a shifter on equation (2), typically exogenous;
$hours$	is the percentage change in hours worked per worker;
f_{HOURS}	is a shifter on equation (3), typically exogenous;
pop	is the percentage change in the regional population;
$frealwage$	is a vertical (regional wage premium) shifter on equation (4);
f_{POP}	is a shifter on equation (4);
$shwrkage$	is the percentage change in the share of the regional population that is of working age;
$employ$	is the percentage change in regional employment;
α_{PPRATE}	is the elasticity of the regional participation rate to the real wage;
$\alpha_{EMPRATE}$	is the elasticity of the regional employment rate to the real wage;
α_{HOURS}	is the elasticity of hours worked per worker to the real wage; and
α_{POP}	is the elasticity of regional population to the real wage.

A short-run closure of equations (1) – (5) has f_{PPRATE} , $f_{EMPRATE}$, f_{HOURS} , $frealwage$, pop , and $shwrkage$ exogenous, with $pprate$, $emprate$, $hours$, f_{POP} and $employ$ endogenous. $realwage$ is determined endogenously in ORANI-R, but largely outside the system of equations (1) – (5). Under this labour market closure, regional population is fixed. This largely ties-down regional employment via equation (5). However some scope for short-run regional employment change is nevertheless provided by equations (1) – (3). These allow for short-run movements in participation, the employment rate, and hours worked per worker, in response to movements in the real consumer wage. The long-run labour market closure is identical to the short-run closure in all respects other than provision for regional population to be a positive function of the regional real wage via activation of equation (4). Equation (4) is activated by exogenous determination of f_{POP} and endogenous determination of pop .

2.2.2 The price of interstate and foreign imports.

We assume that foreign import supply schedules to the U.S. as a whole are upward sloping. As such, foreign import supply schedules to any region in the U.S. are also upward sloping. In like fashion, we assume that inter-regional import supply schedules to any region within the U.S. are upward sloping. This reflects resource constraints in the rest of the U.S. economy. We implement upward sloping import supply schedules for each commodity, c , via equation (6):

$$(6) \quad p_{c,s}^{(0)t} = \eta_{c,s}^t [GDP_r / GDP_{US}] x_{c,s}^{(0)} \quad (s = \text{rest-of-U.S., foreign})$$

$$(t = \text{short-run, long-run})$$

where:

- $p_{c,s}^{(0)t}$ is the percentage change in the basic price of commodity c from foreign and rest-of-U.S. sources over length of run t .
- $\eta_{c,s}^t$ is the reciprocal of the elasticity of supply of imported commodity c from source s over length of run t . For $\eta_{c,foreign}^t$ we use USAGE database values for the elasticity of U.S. foreign import prices to U.S. import demand. For $\eta_{c,rest-of-U.S.}^{short-run}$ we derive short-run U.S. commodity-specific supply elasticities from the USAGE database via the formula of Dixon *et al.* (1982: 309). For long-run applications we set $\eta_{c,rest-of-U.S.}^{long-run}$ at one third of its short-run value.
- GRP_r / GDP_{US} is the ratio of regional GDP in the region for which the ORANI-R model is implemented relative to total U.S. GDP. For example, in the Los Angeles County implementation reported in Sections 3 and 4, this value is 0.037.
- $x_{c,s}^{(0)}$ is the percentage change in demand for commodity c from source s .

2.2.3 Imperfect substitution between commodity varieties.

The ORANI-G model identifies two commodity sources: domestic and foreign. ORANI-R identifies three commodity sources: local, interregional and foreign. In ORANI-R, imperfect substitution between competing sources for the same commodity is modelled via CRESH aggregation functions (Hanoch, 1971)⁴.

2.2.4 Interstate and foreign export demand.

Prices of regional exports, foreign and domestic, are determined via constant elasticity export demand functions, as follows:

$$(7) \quad x_{c,d}^{(4)} = \eta_{c,d}^{(4)} \times p_{c,d}^{(4)}$$

where

- $x_{c,d}^{(4)}$ is the percentage change in the volume of regional exports of c to destination d ($d = \text{rest-of-US (RUS), foreign}$);
- $\eta_{c,d}^{(4)}$ is the price elasticity of demand for exports of commodity c to destination d ; and
- $p_{c,d}^{(4)}$ is the percentage change in the purchaser's price of commodity c in destination d .

⁴ Use of CRESH to model commodity-sourcing in a multi-regional framework was first made by Madden (1996).

In evaluating $\eta_{c,RUS}^{(4)}$, we assume that agents in the rest of the U.S. (RUS) face CRESH substitution possibilities across three commodity sources: the ORANI-R region, the rest of the U.S., and overseas. This is consistent with the modelling of commodity sourcing for agents within the region of ORANI-R implementation (see 2.2.3 above). With demands for the region's commodities determined via CRESH aggregation functions in the rest of the U.S., demands for the region's exports in the rest of the U.S. (RUS) are determined by⁵:

$$(8) \quad x_{c,RUS}^{(4)} = x_c^{(RUS)} - \sigma_{c,interregional}^{(RUS)} (\Phi_{c,RUS}^{(4)} p_{c,RUS}^{(4)} - S_c^{(RUS)} \Phi_{c,RUS}^{(4)} p_{c,RUS}^{(4)})$$

where,

- $x_{c,RUS}^{(4)}$ is the percentage change in the region's exports of good c to the rest of the U.S. (RUS);
- $x_c^{(RUS)}$ is the percentage change in demand for good c in the rest of the U.S. (RUS), undifferentiated by source;
- $\sigma_{c,interregional}^{(RUS)}$ is the CRESH substitution elasticity in the rest of the U.S. (RUS) for good c sourced from the region of focus;
- $\Phi_{c,RUS}^{(4)}$ is the share of the f.o.b price of inter-regional export c in the purchaser's price of c in the rest of the U.S (RUS);
- $p_{c,RUS}^{(4)}$ is the percentage change in the f.o.b. price of good c exported to the rest of the U.S. (RUS) from the region of focus; and
- $S_c^{(RUS)}$ is the share of good c from the region of focus in total usage of good c in the rest of the U.S. (RUS).

Assuming $x_c^{(RUS)}$ is independent of activity in the region of focus, equation (8) implies an inter-regional export demand elasticity for good c of:

$$(9) \quad \eta_{c,RUS}^{(4)} = -\sigma_{c,interregional}^{(RUS)} \Phi_{c,RUS}^{(4)} (1 - S_c^{(RUS)})$$

In evaluating (9), the CRESH substitution elasticity on cross-border intra-U.S. sourcing in the rest of the U.S. ($\sigma_{c,interregional}^{(RUS)}$) is set at the same value as that in the region of focus⁶. The share of the f.o.b price of c in the purchaser's price ($\Phi_{c,RUS}^{(4)}$) is set at 0.8. The share of c in the rest of the U.S. that is sourced from the region of focus ($S_c^{(RUS)}$) is evaluated via comparison of USAGE values for U.S. demand for c and IMPLAN values for inter-regional exports of c by the region of focus.

⁵ See Dixon et al. (1992: 128) for derivation of the percentage change form of cost-minimising CRESH input demands.

⁶ In the application reported in Section 4, this elasticity is set at 3.

In evaluating $\eta_{c,foreign}^{(4)}$, use is made of commodity-specific export demand elasticities from the economy-wide model USAGE. At the same time, a floor is placed on the potential elasticity value via an assumption that agents in other countries face CES inter-regional substitution possibilities. Hence, $\eta_{c,foreign}^{(4)}$ is set via:

$$(10) \quad \eta_{c,foreign}^{(4)} = \text{MAX}[\eta_c^{(4)USAGE} \times [V_c^{(4)USA} / V_c^{(4)REG}], -6.4]$$

where:

$\eta_c^{(4)USAGE}$ is the foreign export demand elasticity for commodity c in the USAGE model.

A typical value for $\eta_c^{(4)USAGE}$ is -3.

$V_c^{(4)USA}$ is the national value of U.S. exports of c .

$V_c^{(4)REG}$ is the value of foreign exports of c by the region of focus.

A floor of -6.4 is set on foreign export demand elasticities by reference to Anderson *et al.* (2008). They show that if foreign agents face sourcing substitution possibilities described by the World Bank's LINKAGE model (van der Mensbrugge 2005), the minimum export demand elasticity is given by $\phi_i^{(2)} S_i^{FOB}$, where $\phi_i^{(2)}$ is the elasticity of substitution between alternative foreign sources of supply for imported good i , and S_i^{FOB} is the share of the f.o.b price in the foreign country purchaser's price of good i ⁷. A typical LINKAGE value for $\phi_i^{(2)}$ is 8. With S_i^{FOB} set at 0.8, this establishes the -6.4 floor on commodity-specific foreign export demand elasticities in equation 10.

3. CONSTRUCTION OF AN ORANI-R DATABASE FROM IMPLAN DATA

The ORANI-R model described in Section 2 has the following characteristics:

1. the structure of capital formation is distinguished by industry;
2. there are three sources of commodity supply: local, rest of U.S., and foreign;
3. there are two export destinations: rest of U.S., and foreign;
4. public consumption is distinguished by whether it is undertaken by the regional government or the federal government; and
5. purchasers' prices differ from basic prices by the value of margins and indirect taxes.

An initial solution to such a model is provided by a balanced input-output table with the following characteristics:

1. a basic price valuation basis;
2. use of services as margins distinguished from direct use of those commodities;
3. investment demand disaggregated by industry;
4. public consumption demand distinguished by government;
5. export demand distinguished by destination; and

⁷ See Anderson *et al.* (2008) pages 29-31.

6. commodity, source and user specific taxes and margins.

Such an input-output table is described by Figure 8. Sections 3.1 – 3.8 describe steps in constructing such a table, using IMPLAN producer price tables and relevant shares from the USAGE database.

3.1. Step 1: A single region producer price IO table from IMPLAN

Figure 1 reports the structure of the disaggregated single-region input-output table that can be constructed from IMPLAN data. The table is at producer prices, with disaggregated treatment of imports but aggregated treatment of margins.

Figure 1: IMPLAN Single region input-output table. Producer prices, with disaggregated treatment of imports and aggregated treatment of margins

VPRD1(c,s,j)	VPRDF ^(A) (c,s,t)
VLAB(j)	
VCAP(j)	
VTAX(j)	
VPRDMAKE(c,j)	

where:

- VPRD1(c,s,j) is value, at producer prices, of commodity ($c \in \text{COM}$) from source ($s \in \text{SRC}$) used by industry ($j \in \text{IND}$) for input to current production;
- VPRDF^(A)(c,s,t) is value, at producer prices, of commodity ($c \in \text{COM}$) from source ($s \in \text{SRC}$) used by final demand category ($t \in \text{FINA}$);
- VLAB(j) are gross payments to labour by industry ($j \in \text{IND}$);
- VCAP(j) are gross payments to capital by industry ($j \in \text{IND}$);
- VTAX(j) are indirect tax payments attributed to sales by industry ($j \in \text{IND}$);
- VPRDMAKE(c,j) is output of commodity ($c \in \text{COM}$) by industry ($j \in \text{IND}$), valued at producer prices.

and where relevant set definitions are:

- COM: All commodities, length 436.
- SRC: All sources, length 3: local, rest of U.S. and foreign.
- IND: All industries, length 436.

FINA: All final demanders, length 7: investment, households, U.S. exports, foreign exports, federal government, state government, stocks.

INST: A subset of FINA, consisting of non-export final demand categories: households, federal government, state government, investment and stocks.

The table is evaluated using input from the IMPLAN 26 file report, the structure of which is described in the MIG IMPLAN Technical Report TR-98002, pp3-4. The mapping between the components of the IMPLAN SAM output Tables 1-3 and Figure 1 above is:

VPRD1(COM, <i>local</i> , IND)	Cell 2 x 1: Domestic use of commodities by industries or payments to commodities.
VPRD1(COM, <i>rest of U.S.</i> , IND)	Cell 8 x 1: Industry domestic import use.
VPRD1(COM, <i>foreign</i> , IND)	Cell 7 x 1: Industry foreign import use.
VPRDF(COM, <i>local</i> , INST)	Cell 2 x 4: Domestic institutional use or final demands by institution.
VPRDF ^(A) (COM, <i>rest of U.S.</i> , INST)	Cell 8 x 4: Institutional domestic import use.
VPRDF ^(A) (COM, <i>foreign</i> , INST)	Cell 7 x 4: Institutional foreign import use.
VPRDF ^(A) (COM, <i>local</i> , <i>U.S. exports</i>)	Cell 1 x 6: Total domestic commodity exports.
VPRDF ^(A) (COM, <i>local</i> , <i>foreign exports</i>)	Cell 1 x 5: Total foreign commodity exports.
VLAB(IND), VCAP(IND), VTAX(IND)	Cell 3 x 1: Factors, distinguishing value-added elements: employee compensation (VLAB), proprietary income and other property type income (VCAP) and indirect business taxes (VTAX).
VPRDMAKE (COM,IND)	Cell 1 x 2: Domestic industry make.

The IMPLAN data follows a producer price valuation basis. Use of commodities as margin services are not distinguished from their direct use. The IMPLAN data are based on BEA national IO data. As such, they replicate the misallocation of indirect taxes in the BEA national IO data. In the BEA IO data, most indirect taxes are attributed to the institutions *collecting* the taxes, not the institutions *producing* the commodities on which the taxes are levied, as conventionally required by a producer price valuation basis. Hence, most taxes appear on output of the retail and wholesale margin industries (Dixon and Rimmer 2002). To allow this tax misallocation to flow into the CGE database will cause at least two problems when the CGE model is used for applied policy analysis:

- (a) CGE model results for welfare measures will be incorrect, because indirect tax wedges are allocated to the wrong commodities.
- (b) CGE model results for shocks to indirect tax rates will generate perverse industrial composition effects.

Correction of BEA misallocation of indirect taxes is among the tasks in transforming the IMPLAN data described by Figure 1 to the ORANI-R data described by Figure 8. The following sections describe how:

- (a) the IMPLAN producer price table is converted to a basic price table;
- (b) independent data is used to re-estimate tax rates and generate tax matrices; and
- (c) independent data are used to estimate margin matrices.

Step 2 begins by converting the IMPLAN data to a basic price valuation basis.

3.2. Step 2: Conversion of the IMPLAN producer price table to a basic price table

Figure 2: Single region input-output table. Basic prices, with disaggregated treatment of imports and aggregated treatment of margins

VBAS1(c,s,j)	VBASF ^(A) (c,s,t)	
VTAX1(c,s,j)	VTAXF ^(A) (c,s,t)	
VLAB(j)		
VCAP(j)		
<table border="1" style="border-collapse: collapse; width: 100%; text-align: center;"> <tr> <td style="padding: 5px;">VBASMAKE(c,j)</td> </tr> </table>		VBASMAKE(c,j)
VBASMAKE(c,j)		

In moving from Figure 1 to Figure 2, we begin by noting that in Figure 1 $V1PRDMAKE_{c,j}$ is the value at producer prices of output of commodity c by industry j . We begin by defining $TAXMAKE_{c,j}$, the value of indirect taxes in the make matrix, as:

$$(11) \quad TAXMAKE_{c,j} = [VTAX_j / V1TOT1_j] \times V1PRDMAKE_{c,j}$$

where $V1TOT1_j$ is the value at producer prices of industry j 's output, defined as:

$$(12) \quad V1TOT_j = \sum_c \sum_s V1PRD_{c,s,j} + VLAB_j + VCAP_j + VTAX_j$$

We define the make matrix valued as basic prices, $VBASMAKE_{c,j}$, as:

$$(13) \quad VBASMAKE_{c,j} = V1PRDMAKE_{c,j} - TAXMAKE_{c,j}$$

Next, we define ($TAXRATE_c$) a vector of commodity-specific tax rates (defined as shares of producer values represented by indirect tax) implicit in the initial IMPLAN data:

$$(14) \quad TAXRATE_c = \sum_j TAXMAKE_{c,j} / \sum_k V1PRDMAKE_{c,k}$$

We define an array of tax payments on source-specific commodities $VITAX_{c,s,j}$. Tax payments on locally-sourced commodities are defined as:

$$(15) \quad VITAX_{c,local,j} = VPRD1_{c,local,j} \times TAXRATE_c$$

Given the format of the data in Figure 1, we have insufficient information to retrieve a tax matrix on domestic and foreign imports. A proportion of the tax currently allocated to retail and wholesale trade is presumably tax collected on imports. As such, the matrices $VPRD1_{c,foreign,j}$ and $VPRD1_{c,rest\ of\ U.S.,j}$ must already be close to a basic price valuation basis. Hence, for the moment we assume:

$$(16) \quad VTAX1_{c,foreign,j} = VTAX1_{c,rest\ of\ U.S.,j} = 0$$

Intermediate flows at basic prices are now defined as:

$$(17) \quad VBAS1_{c,s,j} = VPRD1_{c,s,j} - VTAX1_{c,s,j}$$

We define tax payments on sales of locally-sourced commodities to final demand as:

$$(18) \quad VTAXF_{c,local,f} = VPRDF_{c,local,f}^{(A)} \times TAXRATE_c$$

Again, we have little information on which to form a judgement on tax paid by final demanders on commodities sourced from the rest of the U.S. or overseas. As such, we initially assume:

$$(19) \quad VTAXF_{c,foreign,j} = VTAXF_{c,rest\ of\ U.S.,j} = 0$$

Purchases by final demanders at basic prices are now defined as:

$$(20) \quad VBASF_{c,s,j} = VPRDF_{c,s,j}^{(A)} - VTAXF_{c,s,j}$$

completing the evaluation of all arrays in Figure 2.

Figure 2 is a balanced input-output table at basic prices with disaggregated treatment of imports. Like Figure 1 from which it is derived, it has a number of limitations:

- (a) Indirect taxes remain miscalculated, since they continue to reflect the BEA/IMPLAN misallocation of indirect taxes to retail and wholesale trade.
- (b) Margins are directly allocated to margin commodity sales in the matrices VBAS1 and VBASF.
- (c) Investment does not have an industry dimension.

In Step 3 we make a first effort at margin disaggregation.

3.3. Step 3: Preliminary identification of margin matrices

Figure 3: Single region input-output table. Basic prices, with disaggregated treatment of imports and incomplete margin disaggregation

VBAS1(c,s,j)	VBASF ^(A) (c,s,t)
VTAX1(c,s,j)	VTAXF ^(A) (c,s,t)
VMAR1(m,j)	VMARF ^(A) (m,t)
VLAB(j)	
VCAP(j)	

VBASMAKE(c,j)

In Figure 3, the basic value of use of margin commodity m by producers ($VMAR1_{m,j}$) and final demanders ($VMARF_{m,j}^{(A)}$) has been removed from the basic value flow matrices $VBAS1_{c,s,j}$ and $VBASF_{c,s,t}^{(A)}$ respectively. As such, for $c = m$, $VBAS1_{c,s,j}$ and $VBASF_{c,s,t}^{(A)}$ contain only direct use of c . Use of c as a margin service appears in the rows of $VMAR1_{m,j}$ and $VMARF_{m,j}^{(A)}$. Generation of Figure 3 is described below.

We define $MARSHARE_{m,u}$ as the share of commodity m by user u that is margin use of m , by user u ($u \in USER$). $USER$, a new set of length 8, is comprised of all elements of FINA plus one new element, *industry*. $MARSHARE_{m,u}$ is evaluated from the full 500 sector USAGE database (Dixon and Rimmer 2002). The USAGE database shares a very similar disaggregated structure to that described by Figure 8. Moreover, in the efforts of Peter Dixon and Maureen Rimmer, the creators of the USAGE database, several person-years of work have gone into considered evaluation of tax and margin matrices. As such, it is an excellent source for the shares required to reconfigure the data presented in Figure 1 to a format described by Figure 8. The construction of the USAGE database is described in Dixon and Rimmer (2002).

Using $MARSHARE_{m,u}$, we define the margin matrices $VMAR1_{m,j}$ and $VMARF_{m,j}^{(A)}$ as:

$$(21) \quad VMAR1_{m,j} = VBAS1_{m,local,j} \times MARSHARE_{m,industry} \quad (m \in MAR)$$

$$(22) \quad VMARF_{m,t}^{(A)} = VBASF_{m,local,t}^{(A)} \times MARSHARE_{m,t} \quad (m \in MAR)$$

With $VMAR1_{m,j}$ and $VMARF_{m,j}^{(A)}$ now recording margin usage of commodity m , such usage must be removed from the direct value matrices $VBAS1_{c,s,j}$ and $VBASF_{c,s,t}$:

$$(23) \quad VBAS1_{m,local,j}^{NEW} = VBAS1_{m,local,j}^{OLD} - VMAR1_{m,j} \quad (m \in MAR)$$

$$(24) \quad VBASF_{m,local,j}^{(A)NEW} = VBASF_{m,local,j}^{(A)OLD} - VMARF_{m,j} \quad (m \in MAR)$$

For non-margin commodities, we define the set $NOTMAR = COM - MAR$, and define direct value matrices:

$$(25) \quad VBAS1_{m,local,j}^{NEW} = VBAS1_{m,local,j}^{OLD} \quad (m \in NOTMAR)$$

$$(26) \quad VBASF_{m,local,j}^{(A)NEW} = VBASF_{m,local,j}^{(A)OLD} \quad (m \in NOTMAR)$$

Figure 3 is a balanced input-output table at basic prices with disaggregated treatment of imports and aggregated treatment of margins. The table has a number of limitations:

- (a) Indirect taxes remain miscalculated, since they continue to reflect the BEA/IMPLAN misallocation of indirect taxes to retail and wholesale trade.
- (b) Margins are separately identified, but are not yet allocated to source-specific commodity flows.
- (c) Investment does not have an industry dimension.

In Step 4, the investment column of Figure 3 is disaggregated in the industry dimension.

3.4. Step 4: Disaggregation of investment by industry

Figure 4: Single region input-output table. Basic prices, with disaggregated treatment of imports, identification of investment by industry, and incomplete margin disaggregation

VBAS1(c,s,j)	VBAS2(c,s,j)	VBASF ^(B) (c,s,t)
VTAX1(c,s,j)	VTAX2(c,s,j)	VTAXF ^(B) (c,s,t)
VMAR1(m,j)	VMAR2(c,s,j,m)	VMARF ^(B) (m,t)
VLAB(j)		
VCAP(j)		
VBASMAKE(c,j)		

In Figure 3, we possess information on only aggregate investment in the region, via matrices $VBASF_{c,s,investment}^{(A)}$, $VTAXF_{c,s,investment}^{(A)}$ and $VMARF_{m,investment}^{(A)}$. In Step 4, we identify an industry dimension to investment. In doing so, we create a new set of final demand categories FINB. FINB contains all elements of FINA, other than *investment*.

We begin by calculating aggregate regional investment in the IMPLAN database, ITOT:

$$(27) \quad ITOT = \sum_c \sum_s [VBASF_{c,s,investment}^{(A)} + VTAXF_{c,s,investment}^{(A)}] + \sum_m VMARF_{m,investment}^{(A)}$$

We define industry-specific investment/capital ratios, IKR_j . These are evaluated using USAGE database values. Using IKR_j , we calculate target values for investment by industry I_j as follows:

$$(28) \quad I_j = \left[\{VCAP_j \times IKR_j\} / \sum_k \{VCAP_k \times IKR_k\} \right] \times ITOT$$

The USAGE database recognises that inputs to capital formation differ across industries. Using USAGE database shares, we calculate $B2_{c,s,j}$, the share of industry j 's investment represented by the basic value of inputs of commodity c from source s ⁸. $B2_{c,s,j}$ is then used to calculate initial values for the basic values of inputs to industry j 's capital formation as follows:

⁸ USAGE is a national model and as such recognises two sources, domestic and foreign. In building the regional database, we assume the foreign import shares are the same as the USAGE foreign import shares. We split the USAGE domestic import share into local and rest-of-U.S. components using commodity-specific local / rest-of-U.S. ratios from Figure 3.

$$(29) \text{VBAS2}_{c,s,j} = I_j \times B2_{c,s,j}$$

To calculate investment tax matrices, we begin by evaluating from the USAGE database $T2_{c,s,j}$, the rate of indirect tax on inputs of source-specific commodity c,s to capital formation by industry j . $T2_{c,s,j}$ is then used to calculate initial values for indirect tax collected on inputs to capital formation as follows:

$$(30) \text{VTAX2}_{c,s,j} = \text{VBAS2}_{c,s,j} \times T2_{c,s,j}$$

To calculate investment margin matrices, we begin by evaluating from the USAGE database $M2_{c,s,j,m}$, the ratio of use of margin commodity m to the basic value of inputs of source-specific commodity c,s to capital formation by industry j . $M2_{c,s,j,m}$ is then used to calculate initial values for margin services required to facilitate purchases of source-specific inputs to capital formation by each industry as follows:

$$(31) \text{VMAR2}_{c,s,j,m} = \text{VBAS2}_{c,s,j} \times M2_{c,s,j,m}$$

Figure 4 is now imbalanced. The imbalance arises because, in applying USAGE shares to assumed values for industry-specific total investment, we have as yet done nothing to ensure that the sum across investors of source-specific commodity demands corresponds to the values given in Figure 3. In compiling the database, one option might be to impose balance at this step via a RAS procedure. However the imbalance introduced in this step has no direct consequences for subsequent data manipulations. Hence, we leave the imbalance for the moment, and correct via RAS at the end of Step 8. The database described by Figure 4 has two other limitations:

- (a) Indirect taxes remain miscalculated for all non-investment users, since they continue to reflect the BEA/IMPLAN misallocation of indirect taxes to retail and wholesale trade.
- (b) Margins are separately identified, but are allocated to source-specific commodity flows for investment users only.

In Step 5, we seek to improve the tax and margin matrices relating to intermediate input purchases.

3.5. Step 5: Construction of tax and margin matrices related to intermediate inputs

Figure 5: Single region input-output table. Basic prices, with disaggregated treatment of imports, identification of investment by industry, and detailed margin disaggregation for inputs to production and capital formation.

VBAS1(c,s,j)	VBAS2(c,s,j)	VBASF ^(B) (c,s,t)
VTAX1(c,s,j)	VTAX2(c,s,j)	VTAXF ^(B) (c,s,t)
VMAR1(c,s,j,m)	VMAR2(c,s,j,m)	VMARF ^(B) (m,t)
VLAB(j)		
VCAP(j)		
VBASMAKE(c,j)		

At the beginning of Step 5, taxes on intermediate inputs $VTAX1_{c,s,j}$ continue to reflect the implicit BEA/IMPLAN rates derived in Step 2. As such, $VTAX1_{c,s,j}$ presently reflects the misallocation of indirect taxes discussed in Section 3.1. In Step 5, we reevaluate $VTAX1_{c,s,j}$. We begin by evaluating from the USAGE database $T1_{c,s,j}$, the rate of indirect tax on inputs of source-specific commodity c,s to current production by industry j . $T1_{c,s,j}$ is then used to calculate initial values for indirect tax collected on inputs to current production as follows:

$$(32) \quad VTAX1_{c,s,j} = VBAS1_{c,s,j} \times T1_{c,s,j}$$

To calculate matrices of margins on inputs to current production, we begin by evaluating from the USAGE database $M1_{c,s,j,m}$, the ratio of use of margin commodity m to the basic value of inputs of source-specific commodity c,s to current production by industry j . $M1_{c,s,j,m}$ is then used to calculate initial values for margin services required to facilitate purchases of source-specific inputs to current production by each industry as follows:

$$(33) \quad VMAR1_{c,s,j,m} = VBAS1_{c,s,j} \times M1_{c,s,j,m}$$

The input-output table described by Figure 5 begins Step 5 imbalanced. Inputting the new matrices $VTAX1_{c,s,j}$ and $VMAR1_{c,s,j,m}$ into Figure 5 generates further imbalance in the industry cost and value of margin commodity sales dimensions. Again, in compiling the database, one option might be to impose balance at this step via a RAS procedure. Instead, since the imbalance has no direct consequences for subsequent data processing

steps, we leave the imbalance for the moment, and correct via RAS at the end of Step 8. The database described by Figure 5 has two other limitations:

- (a) Indirect taxes remain miscalculated for all final demands, since they continue to reflect the BEA/IMPLAN misallocation of indirect taxes to retail and wholesale trade.
- (b) Margins are not yet associated with source-specific commodity flows for sales to final demand.

3.6. Step 6: Construction of tax and margin matrices related to private consumption

In Figure 6 we begin by identifying household consumption at basic prices, as follows:

$$(34) V3BAS_{c,s} = VBASF_{c,s,households}^{(B)}$$

Next, we reevaluate tax and margin rates on purchases by households. At the beginning of Step 6, taxes on intermediate inputs $VTAX3_{c,s}$ continue to reflect the implicit BEA/IMPLAN rates derived in Step 2. As such, $VTAX3_{c,s}$ presently reflects the misallocation of indirect taxes discussed in Section 3.1. In Step 6, we reevaluate $VTAX3_{c,s}$. We begin by evaluating from the USAGE database $T3_{c,s}$, the rate of indirect tax on consumption of source-specific commodity c,s by households. $T3_{c,s}$ is then used to calculate initial values for indirect tax collected on inputs to current production as follows:

$$(35) VTAX3_{c,s} = VBAS3_{c,s} \times T3_{c,s}$$

Figure 6: Single region input-output table. Basic prices, with disaggregated treatment of imports, identification of investment by industry, and detailed margin disaggregation for inputs to production, capital formation and household consumption.

$VBAS1(c,s,j)$	$VBAS2(c,s,j)$	$VBAS3(c,s)$	$VBASF^{(C)}(c,s,t)$
$VTAX1(c,s,j)$	$VTAX2(c,s,j)$	$VTAX3(c,s)$	$VTAXF^{(C)}(c,s,t)$
$VMAR1(c,s,j,m)$	$VMAR2(c,s,j,m)$	$VMAR3(c,s,m)$	$VMARF^{(C)}(m,t)$
$VLAB(j)$			
$VCAP(j)$			
$VBASMAKE(c,j)$			

To calculate matrices of margins on purchases by households, we begin by evaluating from the USAGE database $M3_{c,s,m}$, the ratio of use of margin commodity m to the basic value of purchases of source-specific commodity c,s for current private consumption. $M3_{c,s,m}$ is then used to calculate initial values for margin services required to facilitate purchases of source-specific inputs to current production by each industry as follows:

$$(36) \text{VMAR3}_{c,s,m} = \text{VBAS3}_{c,s} \times M3_{c,s,m}$$

The input-output table described by Figure 6 begins Step 6 imbalanced. Inputting the new matrices $\text{VTAX3}_{c,s}$ and $\text{VMAR3}_{c,s,m}$ into Figure 6 generates further imbalance in the aggregate household consumption and value of margin commodity sales dimensions. Again, in compiling the database, one option might be to impose balance at this step via a RAS procedure. Instead, since the imbalance has no direct consequences for subsequent data steps, we leave the imbalance for the moment, and correct via RAS at the end of Step 8. The database described by Figure 6 has two other limitations:

- (a) Indirect taxes remain miscalculated for all final demands other than household consumption, since they continue to reflect the BEA/IMPLAN misallocation of indirect taxes to retail and wholesale trade.
- (b) Margins are not yet associated with source-specific commodity flows for sales to all final demands other than private consumption.

3.7. Step 7: Construction of tax and margin matrices related to destination-specific exports

Figure 7: Single region input-output table. Basic prices, with disaggregated treatment of imports, identification of investment by industry, and detailed margin disaggregation for inputs to production, capital formation, household consumption, and exports.

$\text{VBAS1}(c,s,j)$	$\text{VBAS2}(c,s,j)$	$\text{VBAS3}(c,s)$	$\text{VBAS4}(c,s,d)$	$\text{VBASF}^{(D)}(c,s,t)$
$\text{VTAX1}(c,s,j)$	$\text{VTAX2}(c,s,j)$	$\text{VTAX3}(c,s)$	$\text{VTAX4}(c,s,d)$	$\text{VTAXF}^{(D)}(c,s,t)$
$\text{VMAR1}(c,s,j,m)$	$\text{VMAR2}(c,s,j,m)$	$\text{VMAR3}(c,s,m)$	$\text{VMAR4}(c,s,d,m)$	$\text{VMARF}^{(D)}(m,t)$
$\text{VLAB}(j)$				
$\text{VCAP}(j)$				
$\text{VBASMAKE}(c,j)$				

In Figure 7 we begin by identifying destination-specific exports at basic prices, as follows:

$$(37) \quad V4BAS_{c,d} = VBASF_{c,local,d}^{(C)} \quad (d = \text{inter-regional exports, foreign exports})$$

Next, we reevaluate tax and margin rates on exports. At the beginning of Step 7, taxes on intermediate inputs $VTAX4_{c,d}$ continue to reflect the implicit BEA/IMPLAN rates derived in Step 2. As such, $VTAX4_{c,d}$ presently reflects the misallocation of indirect taxes discussed in Section 3.1. In Step 7, we reevaluate $VTAX4_{c,d}$. We begin by evaluating from the USAGE database $T4_{c,d}$, the rate of indirect tax on exports of commodity c to region d . For $T4_{c,foreign}$ we use USAGE tax rates on foreign exports. For $T4_{c,U.S. \text{ exports}}$ we use a sales-weighted average of USAGE indirect tax rates on domestic commodity sales. $T4_{c,d}$ is used to calculate initial values for indirect tax collected on destination-specific exports as follows:

$$(38) \quad VTAX4_{c,d} = VBAS4_{c,d} \times T4_{c,d}$$

To calculate matrices of margins on destination-specific exports, we begin by evaluating from the USAGE database $M4_{c,d,m}$, the ratio of use of margin commodity m to the basic value of exports of commodity c to destination d . $M4_{c,d,m}$ is then used to calculate initial values for margin services required to facilitate destination-specific exports as follows:

$$(39) \quad VMAR4_{c,d,m} = VBAS4_{c,d} \times M4_{c,d,m}$$

Figure 7 begins Step 7 imbalanced. Inputting the new matrices $VTAX4_{c,d}$ and $VMAR4_{c,d,m}$ into Figure 7 generates further imbalance in the aggregate export and value of margin commodity sales dimensions. Again, in compiling the database, one option might be to impose balance at this step via a RAS procedure. Instead, we leave the imbalance for the moment, and correct via RAS at the end of Step 8. The database described by Figure 7 has two other limitations:

- (a) Indirect taxes remain miscalculated on government demands, since they continue to reflect the BEA/IMPLAN misallocation of indirect taxes to retail and wholesale trade.
- (b) Margins are not yet associated with source-specific commodity flows for sales to government.

3.8. Step 8: Construction of tax and margin matrices related to state and federal public consumption

Figure 8: Single region input-output table. Basic prices, with disaggregated treatment of imports, identification of investment by industry, and detailed margin disaggregation for inputs to production, capital formation, household consumption, and exports.

VBAS1(c,s,j)	VBAS2(c,s,j)	VBAS3(c,s)	VBAS4(c,s,d)	VBAS5(c,s,g)	VBAS6(c,s)
VTAX1(c,s,j)	VTAX2(c,s,j)	VTAX3(c,s)	VTAX4(c,s,d)	VTAX5(c,s,g)	
VMAR1(c,s,j,m)	VMAR2(c,s,j,m)	VMAR3(c,s,m)	VMAR4(c,s,d,m)	VMAR5(c,s,g,m)	
VLAB(j)					
VCAP(j)					
VBASMAKE(c,j)					

In Figure 8 we begin by identifying state and federal demands for source-specific commodities for public consumption purposes, as follows:

$$(40) \quad V5BAS_{c,s,\text{federal government}} = VBASF_{c,s,\text{federal government}}^{(D)}$$

$$(41) \quad V5BAS_{c,s,\text{state government}} = VBASF_{c,s,\text{state government}}^{(D)}$$

Next, we reevaluate tax and margin rates on government consumption spending. At the beginning of Step 8, taxes on public consumption ($VTAX5_{c,s,\text{state government}}$ and $VTAX5_{c,s,\text{federal government}}$) continue to reflect the implicit BEA/IMPLAN rates derived in Step 2. As such, $VTAX5_{c,s,\text{state government}}$ and $VTAX5_{c,s,\text{federal government}}$ presently reflect the misallocation of indirect taxes discussed in Section 3.1. In Step 8, we reevaluate $VTAX5_{c,s,\text{state government}}$ and $VTAX5_{c,s,\text{federal government}}$. We begin by evaluating from the USAGE database $T5_{c,s,g}$, the rate of indirect tax on purchases by state and federal governments for public consumption purposes. USAGE identifies only one aggregate government. As such, we use USAGE tax rates on aggregate public consumption to set identical tax rates on source specific purchases by both state and federal governments. $T5_{c,s,g}$ is used to calculate initial values for indirect tax collected on public consumption purposes as follows:

$$(42) \quad VTAX5_{c,s,g} = VBAS5_{c,s,g} \times T5_{c,s,g}$$

To calculate matrices of margins on public consumption of source-specific commodities, we begin by evaluating from the USAGE database $M5_{c,s,d,m}$, the ratio of use of margin commodity m to the basic value of consumption of c,s by government d . $M5_{c,s,d,m}$ is then used to calculate initial values for margin services required to facilitate government consumption purchases as follows:

$$(43) \text{VMAR5}_{c,s,d,m} = \text{VBAS5}_{c,s,d} \times M5_{c,s,d,m}$$

Finally, the only remaining final demand element of $\text{VBASF}_{c,s,d}^{(D)}$ is $\text{VBASF}_{c,s,\text{stocks}}^{(D)}$. In Figure 8 we make this explicit via:

$$(44) \text{V6BAS}_{c,s} = \text{VBASF}_{c,s,\text{stocks}}^{(D)}$$

Figure 8 begins Step 8 imbalanced. Inputting the new matrices $\text{VTAX5}_{c,s,g}$ and $\text{VMAR5}_{c,s,g,m}$ into Figure 8 generates further imbalance in the aggregate public consumption and value of margin commodity sales dimensions. The final database manipulation is imposition of balance via RAS. Step 8 brings us to the end of our input-output table manipulations: Figure 8, a balanced disaggregated basic price table representing an initial solution to the ORANI-R model.

For this paper, Steps 1 – 8 above have been applied to 2007 IMPLAN data for Los Angeles County to produce a 436 sector, 19 margin ORANI-R model. Section 4 uses this model to investigate the short- and long-run consequences for the LA County economy of primary factor productivity growth.

4. SHORT- AND LONG-RUN CONSEQUENCES OF PRODUCTIVITY GROWTH IN THE L.A. COUNTY ECONOMY

4.1 Simulation design

Tables 1 and 2 present short-run and long-run consequences for the LA County regional economy of a 1 per cent improvement in primary factor productivity in all industries other than dwellings services. Productivity improvement is chosen as an illustrative simulation because it is a supply-side shock. IMPLAN data is typically used for regional input/output impact assessments. Input/output analysis is not suitable for analysis of supply-side shocks.

The short-run and long-run labour market closures are as described in Section 2.2.1. In both the short-run and long-run, household consumption spending is assumed to be a fixed proportion of household income.

In the short-run, industry-specific capital stocks are exogenous, with industry-specific rates of return on capital adjusting to clear industry-specific capital markets. In the long-run, rates of return on industry-specific capital are exogenous, with industry-specific

capital stocks endogenous. Long-run industry-specific investment is determined via an assumption of exogeneity in industry-specific gross capital growth rates.

In the short-run, regional and federal government real public consumption spending are exogenous. In the long-run, the ratio of regional and federal government real public consumption spending to real regional private consumption spending is exogenous.

4.2 Short-run consequences of a 1 per cent improvement in primary factor productivity

The shock is a 1 per cent improvement in the productivity of primary factors used in all Los Angeles County industries other than dwellings services. In the short-run, industry-specific capital stocks cannot adjust to the shock. Via equation (5), short-run employment is largely tied-down via the exogeneity of regional population. In the absence of any movement in regional factor employment, a 1 per cent primary factor productivity improvement should increase regional real GDP by 1 per cent (row 1, Table 1). However, with regional employment sticky via short-run exogeneity of regional population (row 4), the productivity improvement causes the regional real consumer wage to increase (row 13). Via equations (1) – (3) this induces small short-run increases in hours worked per worker, participation rates, and employment rates. This accounts for the small short-run increase in regional employment (row 3). The short-run increase in regional employment is responsible for real GDP increasing by more than the 1 percentage point attributable to productivity growth alone (row 1). With capital stocks fixed (row 2), but productivity and employment rising, rates of return on physical capital increase. This accounts for the short-run increase in real investment (row 4). Real private consumption is linked to real income. With real GDP higher (row 1) so too is real regional income. This accounts for the short-run increase in real private consumption spending (row 6). With regional economic activity higher than it would otherwise have been, so too are interregional and overseas imports (rows 10 and 11 respectively). Note that real public consumption spending is unchanged (row 7). As such, real GNE (rows 5 – 7) increases by less than real GDP (row 1). This requires the regional real balance of trade to move towards surplus. Hence, the increases in real regional exports (rows 8 and 9) exceed the increases in real regional imports (rows 10 and 11). Movement towards surplus in the real regional balance of trade requires the regional price level to fall relative to the external price level (row 14). The expansion in regional export volumes involves movement down fixed interregional and international export demand schedules. Hence regional export price fall. The expansion in foreign and inter-regional imports exerts slight upward pressure on regional import prices. Together, these regional trade price movements cause the regional terms of trade to decline relative to what they would otherwise have been (row 15). The decline in the regional terms of trade explains why the increase in real private consumption (row 6) is less than the increase in real regional GDP (row 1).

The LA County implementation of ORANI-R, ORANI-LA, contains 436 industries. Table 2 reports results for these industries aggregated to 15 broad sectors. Consistent with the uniform 1 per cent improvement across industries in primary factor productivity, most industries expand by a little more than 1 per cent. A notable exception is Dwellings (row 10), which experiences no expansion in output. This reflects the exclusion of this sector

from the general increase in productivity experienced by all other sectors. Public administration (row 15) also experiences little output expansion. This reflects the exogeneity of aggregate real public consumption spending (Table 1, row 7). Prospects for the regional Construction sector (row 4) are largely determined by regional investment (row 5, Table 1). With regional real investment expanding by less than real GDP, the regional Construction sector is among the sectors experiencing the lowest expansion in output.

4.3 Long-run consequences of a 1 per cent improvement in primary factor productivity

Column 2 of Tables 1 and 2 report the long-run impacts on the LA County economy of improved primary factor productivity. In the long-run, the regional capital market closure is equivalent to an assumption that the regional economy can source as much capital as required at exogenously determined real rates of return. In the long-run, equation (4) is activated via exogenous determination of f_{POP} and endogenous determination of pop . With very high values for α_{POP} , this is almost equivalent to an assumption that the regional economy can source as much labour as required at an exogenously determined real regional wage. However to reflect location preference, and some feedback to the national real wage from the regional economy, α_{POP} is set at a high, but not infinite, value⁹.

With exogenous regional rates of return, and near exogeneity of the regional real consumer wage, the increase in primary factor productivity generates sizeable long-run increases in employment of capital (row 2) and labour (row 3). However expansion of the long-run regional economy is limited by two factors. First, via equation (4), the regional real wage must rise to attract population from outside the region. This accounts for the long run increase in the LA County real wage (row 13). Second, expansion of the regional economy causes the regional terms of trade to decline (row 15) damping the potential increase in the values of the marginal product of capital and labour.

The increase in LA County primary factor productivity is projected to increase LA County real GDP by 3.1 per cent. Just under 1 percentage point of this increase is directly attributable to the rise in primary factor productivity. The remainder is due to increased employment of capital (row 2) and labour (row 3). The capital / labour ratio increases slightly (compare rows 2 and 3) because the long-run regional real wage must rise to attract population to the regional economy (row 13).

Long-run private consumption is assumed to be a fixed proportion of long-run regional income. Hence, with long-run real regional GDP higher, so too is regional private consumption (row 6). However expansion of the long-run regional economy is associated with import and export expansion (rows 8 – 11) and thus long-run terms of trade decline (row 15). This damps the increase in real (CPI-deflated) income relative to real GDP.

⁹ At present, α_{POP} is set at 5. In the future, we hope to set this parameter at values that reflect (i) the length of run; and (ii) econometric evidence on the elasticity of regional population to movements in regional wage differentials.

This explains why the increase in private consumption (row 5) is less than the increase in real GDP (row 1). The long-run ratio of public to private consumption spending is exogenous. Hence the long-run percentage change in public consumption spending (row 7) is the same as that for private consumption spending (row 6). Hence the increase in real public consumption spending is also less than the increase in real GDP. Long-run industry-specific investment / capital ratios are exogenous. This accounts for why the increase in aggregate real investment (row 5) is very similar to the increase in the aggregate capital stock (row 2). Since productivity growth is contributing about 1 percentage point to the increase in real GDP (row 1) the increase in the capital stock (row 2), and thus so too, investment (row 4), must be less than that of real GDP (row 1). Hence, with real investment, real private consumption, and real public consumption all rising by less than real GDP, the real balance of trade must move towards surplus (rows 8 – 11).

Table 1: Regional macro impacts (percentage change relative to basecase)

	Short-run	Long-run
1. Real GDP	1.06	3.11
2. Capital stock	0.00	2.40
3. Employment	0.20	2.04
4. Population	0.00	1.70
5. Real investment	0.62	2.32
6. Real private consumption	0.61	2.41
7. Real public consumption	0.00	2.41
8. Real interregional exports	1.04	2.21
9. Real overseas exports	2.67	5.68
10. Real interregional imports	0.25	1.12
11. Real overseas imports	0.72	2.07
12. Real inventories	1.42	3.19
13. Real wage	0.20	0.34
14. GDP deflator	-0.82	-1.54
15. Terms of trade	-0.59	-1.20

Table 2: Sectoral impacts (percentage change relative to basecase)

	Short-run	Long-run
1. Agriculture	1.58	3.98
2. Mining	1.19	4.14
3. Utilities	1.00	3.31
4. Construction	0.71	2.61
5. Manufacturing	1.51	3.28
6. Trade	0.91	2.42
7. Transport	1.42	3.33
8. Information	1.00	2.22
9. Finance, insurance	1.23	3.94
10. Dwellings	0.00	2.56
11. Business services	1.47	3.70
12. Health & education	1.32	3.36
13. Arts	1.28	3.24
14. Other services	1.47	3.45
15. Public administration	0.16	2.50

5 CONCLUSIONS

Computable general equilibrium models of sub-national regions are of three types: top-down multi-regional, bottom-up multi-regional, and bottom-up single region. The ORANI-R model developed in this paper is of the latter type. Multi-regional models, whether bottom-up or top-down, are particularly valuable where policy focus is on both the national and regional consequences of an economic shock. However, regional policy makers are often interested in analysis of economic impacts within a single region of focus only. In such cases, maintenance of the modelling overhead associated with a fully integrated multi-regional model may be unnecessary. Where there is interest in results for only one region of a multi-regional model, the benefits of the full multi-regional model lie chiefly in correct modelling of movements in this region's factor prices, factor supplies, import prices and export prices. As discussed in Section 2 of this paper, a satisfactory closure of regional factor markets and foreign and inter-regional commodity markets can be achieved in a single-region setting without resort to the full complexity of an integrated multi-regional model. That is, the functioning of a single regional economy within a multi-regional environment can be replicated in a single-region model via appropriate modelling of import-supply schedules, export demand schedules, and regional factor supply schedules. This is achieved in this paper via additions to the theory of the well-known and widely-used template for detailed single-region CGE modelling, ORANI-G. Using data from IMPLAN, a widely-used data resource for undertaking input-output analysis at the U.S. sub-regional level, the regional CGE model was implemented for Los Angeles County. However, the data construction algorithm underlying the production of the LA-County database will accept input for any IMPLAN region, making the procedure readily generalisable to construction of a single-region bottom-up CGE model for any U.S. region for which IMPLAN produces input-output data. This marriage of two widely-used modelling resources: IMPLAN and ORANI-G,

represents a substantial reduction in entry barriers to bottom-up CGE modelling of U.S. regions.

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